

# Sub- $\Theta$ Hydrodynamic Behavior of Poly( $\alpha$ -methylstyrene) in Cyclohexane

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**ABSTRACT:** The hydrodynamic properties of poly( $\alpha$ -methylstyrene) (P $\alpha$ MS) in cyclohexane from 16 °C below the  $\Theta$  temperature to 10 °C above  $\Theta$  have been investigated by dilute-solution viscometry and photon correlation spectroscopy. Seven near-monodisperse samples covering the range  $5.9 \times 10^4 \leq \bar{M}_w \leq 3.41 \times 10^6$  were used. These data have been analyzed with regard to chain contraction below  $\Theta$  (the so-called "coil-globule" transition). No evidence for the existence of a globular state was found. It is found that the temperature dependencies of chain contraction parameters, based on the intrinsic viscosity  $[\eta]$  and the hydrodynamic radius  $R_H$ , can be expressed in terms of master curves of  $\alpha^3|\tau|M^{1/2}$  versus  $|\tau|M^{1/2}$ , where  $\alpha$  is the chain expansion or contraction factor (from  $[\eta]$  or  $R_H$ ),  $\tau$  is the reduced temperature ( $\tau \equiv (T - \Theta)/\Theta$ ), and  $M$  is molecular weight. An asymptotic region (plateau), generally associated with the collapsed state, is reached with the  $R_H$  data and approached with the  $[\eta]$  data. Attainment of the plateau occurs at higher values of  $\alpha_\eta^3|\tau|M^{1/2}$  than for  $\alpha_H^3|\tau|M^{1/2}$ , where  $\alpha_\eta$  and  $\alpha_H$  are, respectively,  $[\eta]$ - and  $R_H$ -based contraction factors. For polystyrene the reverse order has been observed. These results suggest a strong dependence of polymer contraction on chemical structure.

## Introduction

Although the properties of macromolecules in both good ( $A_2 \gg 0$ , where  $A_2$  is the osmotic second virial coefficient) and  $\Theta$  ( $A_2 = 0$ ) solvents have received vast attention, chain behavior in poor solvents ( $A_2 < 0$ ) has received little attention for many years. Recent theoretical developments<sup>1-7</sup> dealing with the "coil-to-globule" transition have, however, led to a number of experimental studies<sup>8-24</sup> of this problem. The vast majority of these studies<sup>8-23</sup> have dealt with polystyrene (PS), which has the advantage of being readily available in near-monodisperse form over an extremely broad range of molecular weights.

In this work, we report the results of hydrodynamic measurements on dilute solutions of poly( $\alpha$ -methylstyrene) (P $\alpha$ MS) in cyclohexane below the  $\Theta$  temperature. Like PS, P $\alpha$ MS chains of very high molecular weight and low polydispersity can be prepared. In addition, P $\alpha$ MS is known<sup>25</sup> to exhibit a negligible dependence of unperturbed dimensions on temperature, whereas PS exhibits larger unperturbed chain dimensions as the temperature is decreased.<sup>26</sup> In addition, it has been noted<sup>25,27</sup> that P $\alpha$ MS remains in solution at moderate concentrations ( $c \approx 10^{-3}$  g mL<sup>-1</sup>) for high molecular weights well below the  $\Theta$  temperature. For example, Selser<sup>27</sup> found via light scattering that a P $\alpha$ MS sample of  $\bar{M}_w = 976\,000$  showed no signs of aggregation in cyclohexane at 26 °C (ca. 10 °C below  $\Theta$ ) over the concentration range of  $6.6 \times 10^{-4}$  to  $2.21 \times 10^{-3}$  g mL<sup>-1</sup>. It was pointed out by Selser<sup>27</sup> that the "noncollapse" of P $\alpha$ MS was similar to that observed for poly(*p*-chlorostyrene) in *n*-propylbenzene.<sup>28,29</sup> Thus, different polymer-solvent systems appear to exhibit substantially different sub- $\Theta$  behavior.

Recently, results of a photon correlation spectroscopy (PCS) and low-angle, time-averaged light-scattering study of the P $\alpha$ MS-cyclohexane system, including measurements below  $\Theta$ , have appeared.<sup>30</sup> In the present paper, we report the results of both PCS and intrinsic viscosity

**Table I**  
Molecular Characteristics of P $\alpha$ MS Samples

sample	$\bar{M}_w \times 10^{-4}$ <sup>a</sup>	$\bar{M}_n \times 10^{-4}$ <sup>b</sup>	$\bar{M}_w/\bar{M}_n$ <sup>c</sup>	$\bar{M}_z/\bar{M}_w$ <sup>c</sup>
PL-55	5.90	5.38	1.13	1.11
PC-4	11.8	11.5	1.03	1.03
PC-6	30.5	28.9	1.07	1.06
PC-17	66.5	59.4	1.09	1.06
PL-770	90.3		1.05	1.04
PC-16	114		1.11	1.08
JL-4	341		1.15	1.17

<sup>a</sup> Via LALLS. <sup>b</sup> Via membrane osmometry. <sup>c</sup> Via SEC.

experiments conducted below  $\Theta$  for this same system. The present measurements extend the study of the sub- $\Theta$  behavior of P $\alpha$ MS to much greater values of  $|\tau|M^{1/2}$ , where  $\tau$  is the reduced temperature ( $\tau \equiv (T - \Theta)/\Theta$ ) and  $M$  is the molecular weight, than that reported previously.<sup>30</sup> These results permit a comparison of the sub- $\Theta$  contraction of P $\alpha$ MS with that of PS.

## Experimental Section

P $\alpha$ MS standards, prepared by anionic polymerization, were obtained from Polymer Laboratories and Pressure Chemical Co. The highest molecular weight polymer, JL-4, was prepared at the University of Alabama at Birmingham by polymerization in tetrahydrofuran (THF) at -78 °C using high-vacuum techniques<sup>31</sup> with *sec*-butyllithium as initiator. The tacticity of anionically produced P $\alpha$ MS has recently been reported by Cotts and Selser<sup>30</sup> as 53 % syndiotactic, 41 % heterotactic, and 5 % isotactic triads.

Molecular weights and polydispersities were determined by a combination of low-angle laser light scattering (LALLS), membrane osmometry, and size-exclusion chromatography (SEC). Experimental details have been previously reported.<sup>25</sup>

The solvent used in the present work was HPLC grade cyclohexane (Aldrich, 99.9+ % by gas chromatography). Literature values<sup>32</sup> for the physical properties of this solvent were employed. Intrinsic viscosities  $[\eta]$  and Huggins coefficients  $k_H$  were determined via extrapolation of data obtained for several concentrations to infinite dilution using the Huggins equation. In most cases, flow times were manually measured to  $\pm 0.1$  s. The temperature in these experiments was controlled to within  $\pm 0.02$  °C of the desired temperature using a water bath. Solutions and

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**Table II**  
**Intrinsic Viscosities<sup>a</sup> and Huggins Coefficients for P $\alpha$ MS in Cyclohexane**

sample	$\bar{M}_w \times 10^{-4}$	$T = 46\text{ }^\circ\text{C}$		$T = 39\text{ }^\circ\text{C}$		$T = 36\text{ }^\circ\text{C}$		$T = 32\text{ }^\circ\text{C}$		$T = 28\text{ }^\circ\text{C}$		$T = 24\text{ }^\circ\text{C}$		$T = 20\text{ }^\circ\text{C}$	
		$[\eta]$	$k_H$	$[\eta]$	$k_H$	$[\eta]$	$k_H$	$[\eta]$	$k_H$	$[\eta]$	$k_H$	$[\eta]$	$k_H$	$[\eta]$	$k_H$
PL-55	5.90			0.177	0.78	0.176	0.81	0.174	0.88	0.168	1.1	0.164	1.1	0.158	1.5
PC-4	11.8	0.265	0.70	0.253	0.77	0.250	0.76	0.243	0.74	0.235	0.88	0.222	0.94	0.206	1.3
PC-6	30.5	0.440	0.73	0.409	0.78	0.404	0.75	0.379	0.91	0.360	0.95	0.328	1.3	0.298	1.8
PC-17	66.5	0.682	0.63	0.607	0.79	0.591	0.83	0.549	0.88	0.494	1.1	0.439	1.3	0.40	
PL-770	90.3	0.792	0.62			0.695	0.74	0.624	0.86	0.549	1.0	0.50		0.43	
PC-16	114	0.896	0.61			0.761	0.76	0.688	0.86	0.620	1.0	0.56		0.50	

sample	$\bar{M}_w \times 10^{-4}$	$T/^\circ\text{C}$	$[\eta]$
JL-4	341	25	0.85

<sup>a</sup> Units: dL g<sup>-1</sup>.

solvents were filtered directly into Ubbelohde viscometers through 1.0- $\mu\text{m}$  (nominal pore size) Gelman Acrodisc CR filters; concentrations were chosen to give relative viscosities between about 1.1 and about 1.4.

For the highest molecular weight samples at the lowest temperatures, the Schott-Gerate AVS/G automated viscometer was employed. Concentrations used with this unit were at least 1 order of magnitude lower than those used in the manual measurements and were as low as  $1.2 \times 10^{-5}$  g mL<sup>-1</sup> for sample JL-4 ( $\bar{M}_w = 3.41 \times 10^6$ ) at 25  $^\circ\text{C}$ . Measurements were possible at these reduced concentrations because of the greater precision of measurements ( $\pm 0.01$  s) with the Schott unit. This improved reproducibility is due to the automatic timing and superior thermal control (better than  $\pm 0.01$   $^\circ\text{C}$ ) of this unit. Extrapolations to infinite dilution were not necessary because of the extremely low concentrations that were used.

PCS experiments were conducted using a custom-built goniometer,<sup>33,34</sup> a Jodon Model HN-50 helium-neon laser, and a Brookhaven Instruments Co. BI-2030 AT correlator. Measurements were confined to scattering angles of 20 $^\circ$  and 25 $^\circ$ . Solution clarification was accomplished using a closed-loop filtration system.<sup>34</sup> Gelman Acrodisc CR filters of 0.2- and 0.45- $\mu\text{m}$  nominal pore sizes were used. The closed-loop system is especially applicable to measurements in poor solvents. Initially, a measured volume of solvent is continuously filtered until a constant intensity is observed at the detector output. Modest additions of a known volume of stock polymer solution allow the concentration dependence of  $D_{\text{app}}$ , the apparent z-average diffusion coefficient, to be measured from lowest to highest concentrations. The onset of any aggregation would be detected by a marked increase in photon count rate accompanied by a sharp decrease in  $D_{\text{app}}$ . Temperature control was  $\pm 0.1$   $^\circ\text{C}$ .

Intensity correlation functions were converted to electrical correlation functions, which were then analyzed by the method of cumulants<sup>35</sup> to second order. Values of the normalized second moment  $Q$  were, with the exception of sample JL-4, always less than 0.1 and thus substantiate the lack of aggregation. Somewhat larger second-moment values of ca. 0.3 were observed for sample JL-4 at 25  $^\circ\text{C}$ . This result is probably attributable to the extremely low concentration ( $4.8 \times 10^{-6}$  g mL<sup>-1</sup>) used for this sample. Such a low concentration resulted in a poorer signal-to-noise ratio, but appreciably higher concentrations resulted in aggregation and phase separation. It should also be mentioned that the value of  $Q$  will increase with increasing polydispersity (Table I). Pusey<sup>36</sup> has shown that

$$Q + 1 = \bar{M}_w / \bar{M}_v \quad (1)$$

where  $\bar{M}_v$  is the viscosity-average molecular weight. While an increase in  $Q$  is observed, this increase exceeds that based on eq 1. In what follows, the PCS results for the JL-4 sample comprise only one data point. Consequently, the  $Q$  value, although somewhat large for this sample, does not impact the conclusions of this work.

## Results and Discussion

Molecular weights and polydispersity values are presented in Table I. It is seen from these data that samples covering a broad range of molecular weights and exhibiting

**Table III**  
**MHS Parameters for P $\alpha$ MS in Cyclohexane**

$T/^\circ\text{C}$	$K \times 10^4 \text{ }^\circ / (\text{dL g}^{-3/2} \text{ mol}^{1/2})$	$\alpha^a$
46	4.87	0.539
39	6.66	0.508
36	7.47	0.498
32	10.5	0.466
28	14.7	0.434
24	18.9	0.407
20	22.7	0.386

<sup>a</sup>  $K$  and  $\alpha$  values were obtained by linear regression analyses.

**Table IV**  
**Flow Times for P $\alpha$ MS PC-16 ( $\bar{M}_2 = 1.14 \times 10^6$ ) in Cyclohexane at 28  $^\circ\text{C}$  (Concentration =  $3.56 \times 10^{-3}$  g/mL)<sup>a</sup>**

time at 28 $^\circ\text{C}/\text{h}$	flow times/s
0	161.46, 161.48
19	161.47, 161.53
42	161.62, 161.61
66	161.67, 161.69

<sup>a</sup> The solution was sealed into the viscometer using wired-on septa. Septa were removed for flow-time measurements at the indicated time intervals and were then replaced.

narrow and symmetrical molecular weight distributions were used in this work.

$[\eta]$  and  $k_H$  values are collected in Table II; some of these results have been previously reported.<sup>37</sup> The  $[\eta]$  data lead to the Mark-Houwink-Sakurada (MHS) parameters listed in Table III. In all cases the MHS plots were strictly linear with correlation coefficients  $\geq 0.999$ . This finding, along with the absence of any visible turbidity, suggests the absence of any appreciable aggregation. Also, repeated measurements of flow times for some of the solutions (see Table IV) showed no change over periods ranging from 1 to 3 days. Thus, no signs of aggregation were detected in the viscosity experiments.

A progressive decrease in the MHS exponent occurs as the temperature is lowered. The exponent of 0.386 obtained at 20  $^\circ\text{C}$  is believed to be the lowest reported for linear chains. The Huggins coefficient is also sensitive to chain contraction, with average values ranging from  $0.66 \pm 0.05$  at 46  $^\circ\text{C}$  to  $1.5 \pm 0.3$  at 20  $^\circ\text{C}$ . No dependence of  $k_H$  on molecular weight was observed. A theoretical value of 0.99 has been suggested<sup>38</sup> for hard spheres.

The z-average translational diffusion coefficients  $D_z$  and  $k_d$  values were calculated from the concentration dependence of  $D_{\text{app}}$  by the expression

$$D_{\text{app}} = D_z(1 + k_d C) \quad (2)$$

and are listed in Table V. The concentration dependencies of  $D_{\text{app}}$  were strictly linear (Figure 1), again suggesting the absence of aggregation. For sample JL-4 at 25  $^\circ\text{C}$ , the time dependence of the PCS parameters was

**Table V**  
Diffusion Coefficients and Diffusion Virial Coefficients for P $\alpha$ MS in Cyclohexane at  $T < \Theta$

sample	$\bar{M}_w \times 10^{-4}$	$T = 28^\circ\text{C}$		$T = 20^\circ\text{C}$	
		$D_z \times 10^7 / (\text{cm}^2 \text{s}^{-1})$	$-k_d / (\text{mL g}^{-1})$	$D_z \times 10^7 / (\text{cm}^2 \text{s}^{-1})$	$-k_d / (\text{mL g}^{-1})$
PL-55	5.90	4.95	15	4.55	28
PC-4	11.8	3.86	21	3.38	37
PC-6	30.5	2.45	64	2.13	64
PC-17	66.5	1.72	73	1.55	115
PL-770	90.3	1.55	63	1.41	252
PC-16	114	1.35	95	1.33	845

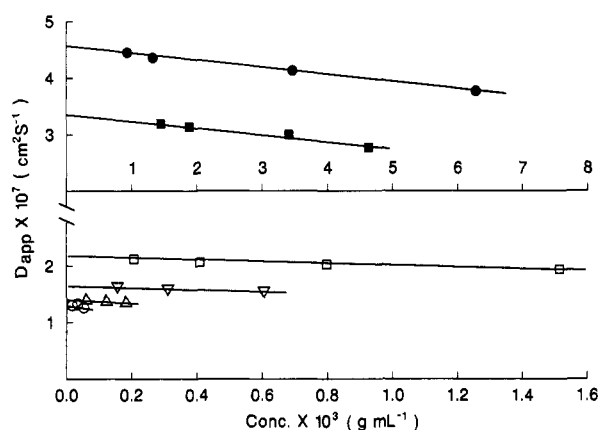
sample	$\bar{M}_w \times 10^{-4}$	$T = 25^\circ\text{C}$ $D_z \times 10^8 \text{ s} / (\text{cm}^2 \text{s}^{-1})$
JL-4	341	9.46

<sup>a</sup> No concentration dependence was measured for this sample.  $D_{\text{app}}$  measured at the extremely low concentration of  $4.8 \times 10^{-6} \text{ g mL}^{-1}$  was assumed to be approximately equivalent to  $D_z$ .

**Table VI**  
Time Dependence of PCS Parameters for P $\alpha$ MS JL-4 in Cyclohexane at  $25^\circ\text{C}$  (Concentration =  $4.8 \times 10^{-6} \text{ g/mL}$ ) over 3 Days

day	$\Gamma$	$Q$
1	$226.6 \pm 6.9^a$	$0.30 \pm 0.03^a$
2	$228.8 \pm 4.6^b$	$0.32 \pm 0.02^b$
3	$227.6 \pm 12.8^c$	$0.33 \pm 0.02$

<sup>a</sup> Average of 10 measurements. <sup>b</sup> Average of 5 measurements. <sup>c</sup> Average of 9 measurements.



**Figure 1.** Concentration dependence of apparent diffusion coefficients for P $\alpha$ MS in cyclohexane at  $20^\circ\text{C}$ . Symbols: ●, PL-55; ■, PC-4; □, PC-6; ▽, PC-17; ▲, PL-770; ○, PC-16.

studied over 3 days (Table VI) to be certain that measured values corresponded to a stable state. Excellent agreement was observed between both decay rate  $\Gamma$  values and second-moment values. These data again substantiate the lack of appreciable aggregation. Attempts to conduct PCS measurements for sample JL-4 at  $24^\circ\text{C}$  ( $c = 4.8 \times 10^{-6} \text{ g mL}^{-1}$ ) resulted in detectable aggregation after 7 h and visible turbidity after 24 h.

Plots of  $\log D_z$  versus  $\log \bar{M}_w$  at 28 and  $20^\circ\text{C}$  yielded the following expressions:

$$D_z^{28^\circ\text{C}} = 6.49 \times 10^{-5} \bar{M}_w^{-0.442} \quad (3)$$

$$D_z^{20^\circ\text{C}} = 4.78 \times 10^{-5} \bar{M}_w^{-0.426} \quad (4)$$

The  $D_z$  and  $k_d$  data at  $28^\circ\text{C}$  are in accord with the findings of Cotts and Selser<sup>30</sup> at  $25^\circ\text{C}$  for the same polymer-solvent system. The  $k_d$  values, like the  $k_H$  values, are quite sensitive to the thermodynamic state, showing an increase

in magnitude in poorer solvents. Unlike  $k_H$ ,  $k_d$  values are also strongly dependent on molecular weight; negative values of  $k_d$  were always obtained under these sub- $\Theta$  conditions.

From the  $D_z$  values, hydrodynamic radii  $R_H$  can be calculated from

$$R_H = kT/6\pi\eta_0 D_z \quad (5)$$

where  $k$  is Boltzmann's constant,  $T$  is the absolute temperature, and  $\eta_0$  is the solvent viscosity.<sup>32</sup> Similarly, equivalent sphere viscometric radii  $R_v$  can be calculated as<sup>39</sup>

$$R_v = ([\eta]M)^{1/3} (10^3/\pi N_A)^{-1/3} \quad (6)$$

where  $M$  is the molecular weight and  $N_A$  is Avogadro's number. Values of  $R_H$  and  $R_v$  at 28 and  $20^\circ\text{C}$  are given in Table VII and double logarithmic plots of these equivalent sphere radii versus molecular weight are shown in Figures 2 and 3.

All values of  $R_v/R_H$  are larger than unity, the value which corresponds to a hard sphere.  $R_v/R_H$  increases with increasing molecular weight and shows no significant temperature dependence on comparing values obtained at 8 and  $16^\circ\text{C}$  below  $\Theta$ . Theory<sup>43-45</sup> predicts an increase in  $R_v/R_H$  on going from good to  $\Theta$  solvents. We are not, however, aware of theoretical predictions for  $R_v/R_H$  below  $\Theta$ , nor are we aware of any predicted molecular weight dependence. Clearly, the  $R_v/R_H$  values indicate that, even in highly contracted states, spherical globular particles are not obtained, at least for the P $\alpha$ MS-cyclohexane system.

The data of Figures 2 and 3 lead to the following power law dependencies:

$$R_H^{28^\circ\text{C}} = 4.01 \times 10^{-2} \bar{M}_w^{0.441} \quad (\text{nm}) \quad (7)$$

$$R_H^{20^\circ\text{C}} = 4.60 \times 10^{-2} \bar{M}_w^{0.426} \quad (\text{nm}) \quad (8)$$

$$R_v^{28^\circ\text{C}} = 2.83 \times 10^{-2} \bar{M}_w^{0.479} \quad (\text{nm}) \quad (9)$$

$$R_v^{20^\circ\text{C}} = 3.36 \times 10^{-2} \bar{M}_w^{0.460} \quad (\text{nm}) \quad (10)$$

Since the radius should scale with  $M^{1/3}$  for polymer globules,<sup>6</sup> the exponent in eqs 7-10 are another strong indication that a globular state is not achieved.

Comparison of the contraction of P $\alpha$ MS in cyclohexane with findings for other systems requires the calculation of chain expansion or contraction factors  $\alpha_\eta$  and  $\alpha_H$  where

$$\alpha_\eta = ([\eta]/[\eta]_\Theta)^{1/3} \quad (11)$$

$$\alpha_H = R_H/R_{H,\Theta} \quad (12)$$

and the subscript  $\Theta$  denotes measurements at the Flory  $\Theta$  temperature. For a typical system exhibiting an upper critical solution temperature, at temperatures above  $\Theta$   $\alpha$  will have values greater than unity, indicative of chain expansion. At temperatures below  $\Theta$ , chain contraction occurs, and  $\alpha$  values are less than 1.  $[\eta]$  scales with molecular weight as

$$[\eta]_\Theta = 7.35 \times 10^{-4} \bar{M}_w^{1/2} \quad (\text{dL g}^{-1}) \quad (13)$$

for P $\alpha$ MS in cyclohexane at the  $\Theta$  temperature ( $36.2^\circ\text{C}$ ).<sup>37</sup> This result is in excellent agreement with data previously reported by Noda and co-workers for the same system.<sup>40</sup>

Table VII  
Hydrodynamic and Viscometric Radii of P $\alpha$ MS in Cyclohexane

sample	$\bar{M}_w \times 10^{-4}$	$T = 28^\circ\text{C}$			$T = 20^\circ\text{C}$		
		$R_H/\text{nm}$	$R_v/\text{nm}$	$R_v/R_H$	$R_H/\text{nm}$	$R_v/\text{nm}$	$R_v/R_H$
PL-55	5.90	5.24	5.39	1.03	4.84	5.28	1.09
PC-4	11.8	6.72	7.60	1.13	6.52	7.27	1.12
PC-6	30.5	10.6	12.0	1.13	10.3	11.3	1.10
PC-17	66.5	15.1	17.3	1.15	14.2	16.1	1.13
PL-770	90.3	16.7	19.9	1.19	15.6	18.4	1.18
PC-16	114	19.2	22.4	1.17	16.6	20.8	1.25

sample	$\bar{M}_w \times 10^{-4}$	$T = 25^\circ\text{C}$		
		$R_H/\text{nm}$	$R_v/\text{nm}$	$R_v/R_H$
JL-4	341	25.7	35.8	1.39

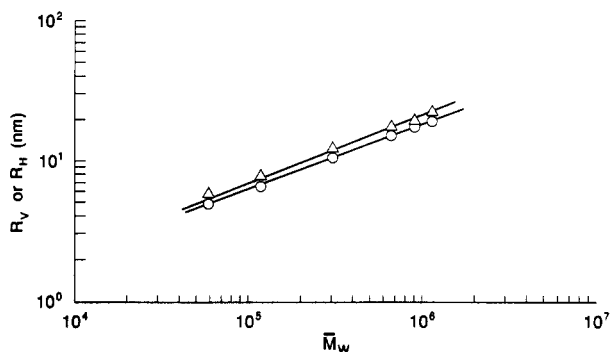


Figure 2. Dependence of  $R_v$  ( $\Delta$ ) and  $R_H$  ( $\circ$ ) on molecular weight for P $\alpha$ MS in cyclohexane at  $28^\circ\text{C}$ .

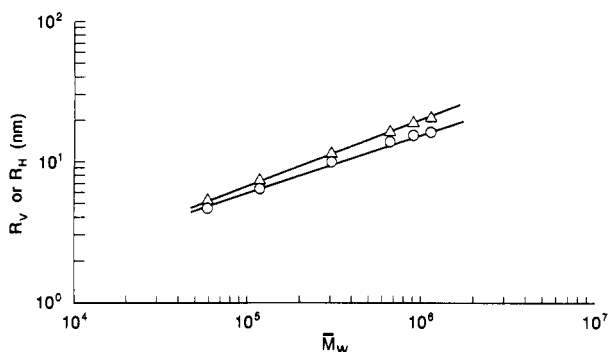


Figure 3. Dependence of  $R_v$  ( $\Delta$ ) and  $R_H$  ( $\circ$ ) on molecular weight for P $\alpha$ MS in cyclohexane at  $20^\circ\text{C}$ .

$R_H$  varies with molecular weight as

$$R_H = 2.12 \times 10^{-2} \bar{M}_w^{1/2} \text{ (nm)} \quad (14)$$

based on the combined  $\Theta$  condition data of Cowie and Bywater at  $37^\circ\text{C}$ <sup>41</sup> and Noda and co-workers at  $34.5^\circ\text{C}$ .<sup>42</sup> Equation 14 is also in agreement with recent data reported by Cotts and Selser<sup>30</sup> for the same system. Thus, chain expansion and contraction ratios may be calculated using the data of Tables II and VII and eqs 13 and 14.

A comparison of the contraction behavior based on hydrodynamic properties for P $\alpha$ MS and polystyrene is given in Figure 4. For PS the recent  $\alpha_\eta$  data of Chu and Wang<sup>23a</sup> are utilized, while the  $\alpha_H$  data are from Vidakovic and Rondelez.<sup>18</sup> These latter data are in excellent agreement with the more recent  $\alpha_H$  determinations by Chu and Wang.<sup>23b</sup> Our  $\alpha_H$  data for P $\alpha$ MS are supplemented by the data of Cotts and Selser.<sup>30</sup>

In plots of  $\alpha^3|\tau|\bar{M}^{1/2}$  versus  $|\tau|\bar{M}^{1/2}$  attainment of a plateau region where the former parameter is independent of the latter has been taken as evidence for reaching the "collapsed state".<sup>17,19-24</sup> For polystyrene this leveling off is seen at  $\alpha_\eta^3|\tau|\bar{M}^{1/2}$  values of about  $24 \text{ g}^{1/2} \text{ mol}^{1/2}$ , cor-

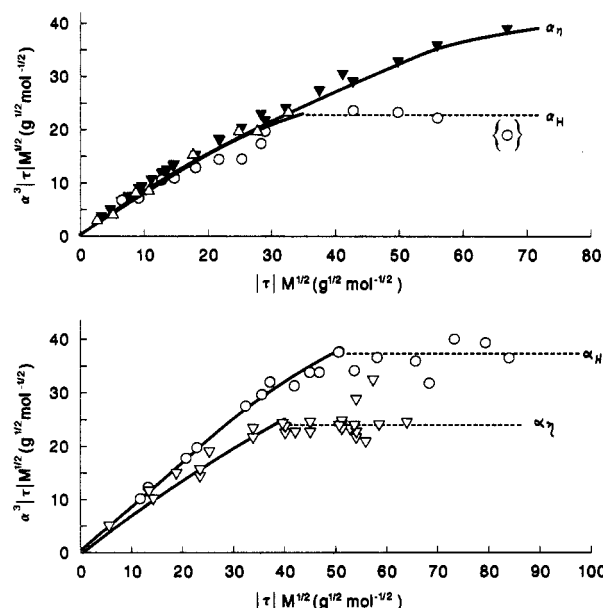
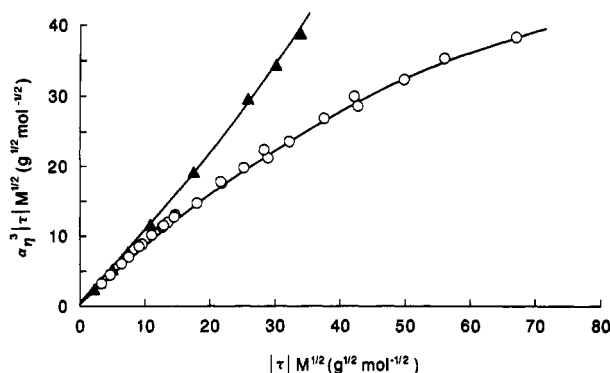


Figure 4. Plot of scaled expansion factor  $\alpha^3|\tau|\bar{M}^{1/2}$  versus scaled reduced temperature  $|\tau|\bar{M}^{1/2}$  for P $\alpha$ MS (top) and PS (bottom) in cyclohexane. For P $\alpha$ MS the symbols are as follows:  $\circ$ ,  $\alpha_H$  data (this work);  $\Delta$ ,  $\alpha_H$  data (ref 30);  $\nabla$ ,  $\alpha_\eta$  data (this work). For PS the symbols are as follows:  $\circ$ ,  $\alpha_H$  data (ref 18);  $\Delta$ ,  $\alpha_\eta$  data (ref 23). The  $\alpha_H$  data point for sample JL-4 at  $25^\circ\text{C}$  is bracketed because of the larger measured  $Q$  value for this sample.

responding to  $|\tau|\bar{M}^{1/2}$  of about  $40 \text{ mol}^{1/2} \text{ g}^{-1/2}$  or greater. Values of  $\alpha_H^3|\tau|\bar{M}^{1/2} \approx 37 \text{ g}^{1/2} \text{ mol}^{1/2}$  are obtained at  $|\tau|\bar{M}^{1/2}$  of about  $50 \text{ g}^{1/2} \text{ mol}^{1/2}$  or greater. For the P $\alpha$ MS-cyclohexane system, the asymptotic value  $\alpha_H^3|\tau|\bar{M}^{1/2} \approx 22 \text{ g}^{1/2} \text{ mol}^{1/2}$  is achieved at  $|\tau|\bar{M}^{1/2} \geq 35 \text{ g}^{1/2} \text{ mol}^{1/2}$ . No clear asymptote is seen for  $\alpha_\eta^3|\tau|\bar{M}^{1/2}$  over the range of  $|\tau|\bar{M}^{1/2}$  values investigated in this work. However, on the basis of available data, a leveling off at  $\alpha_\eta^3|\tau|\bar{M}^{1/2} \approx 40 \text{ g}^{1/2} \text{ mol}^{1/2}$  seems likely for  $|\tau|\bar{M}^{1/2}$  values  $\geq 70 \text{ g}^{1/2} \text{ mol}^{1/2}$ .

The most interesting aspect of Figure 4 is the reversal of the asymptotes for P $\alpha$ MS as compared to those for polystyrene. With P $\alpha$ MS the asymptotic value (assuming it could be attained) for  $\alpha_\eta^3|\tau|\bar{M}^{1/2}$  is much larger than that for  $\alpha_H^3|\tau|\bar{M}^{1/2}$ . For polystyrene this order is reversed. This effect is considerably greater than any conceivable errors in the measurement of  $[\eta]$  or  $D_z$ . For example, the  $[\eta]$  values in this work would have to be reduced by about 50% for the P $\alpha$ MS contraction to track that of PS in Figure 4. Thus, there is little doubt regarding the different contraction behavior of the two types of polymer chains. This disparity of results for these two very similar systems was initially surprising. However, a dependence of polymer contraction on chemical structure is to be expected. Reasons include differences in chain stiffness,<sup>5</sup> short-range correlations, and ternary (three-body) interactions, which



**Figure 5.** Plot of scaled expansion factor  $\alpha_h^3 |\tau| M^{1/2}$  versus scaled reduced temperature  $|\tau| M^{1/2}$  for P $\alpha$ MS in cyclohexane above ( $\blacktriangle$ ) and below ( $\circ$ )  $\Theta$ . Notice that there is only a very limited regime where expansion and contraction are symmetrical. The splitting is interpreted as a consequence of the importance of ternary interactions below (but not above)  $\Theta$ .

are expected to become very important below  $\Theta$ , where hydrodynamic properties appear to be rather sensitive to ternary interactions.<sup>46</sup> Very large differences in the asymptotic "collapse" behavior have also been noted by Chu et al.<sup>20</sup> for polystyrene under different  $\Theta$  conditions. Unusual sub- $\Theta$  behavior has also been noted for other polymer-solvent systems.<sup>29</sup>

Finally, we note that  $[\eta]$  data obtained above  $\Theta$  and those results below  $\Theta$  indicate a very limited regime where the expansion and contraction of the coil is symmetrical (Figure 5). Symmetry is seen only in the region  $-10 \leq |\tau| M^{1/2} \leq 10$ . This splitting and the reasonable linearity of  $\alpha_h^3 |\tau| M^{1/2}$  above  $\Theta$ , where only two-body interactions are expected to contribute significantly to coil expansion, indicate the importance of three-body interactions at temperatures less than  $\Theta$ .

In conclusion, the sub- $\Theta$  contraction of P $\alpha$ MS in cyclohexane has been studied using intrinsic viscosity and PCS experiments. The dependencies of coil radii on molecular weight and the relatively small contractions observed demonstrate conclusively that a collapsed globular state is not reached. Nevertheless, an asymptotic region is observed in the plot of  $\alpha_h^3 |\tau| M^{1/2}$  versus  $|\tau| M^{1/2}$  and approached in the plot of  $\alpha_h^3 |\tau| M^{1/2}$  versus  $|\tau| M^{1/2}$ , similar to that reported by other workers<sup>17,19-24</sup> for different polymer-solvent systems. Significant differences are noted in this asymptotic behavior for different polymers systems.

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## References and Notes

- Ptitsyn, O. B.; Kron, A. K.; Eizner, Y. Y. *J. Polym. Sci., Polym. Phys. Ed.* 1968, 16, 3509.
- Eizner, Y. Y. *Polym. Sci. USSR* 1972, 14, 1695.
- de Gennes, P. G. *J. Phys. Lett.* 1975, 36, L55; 1978, 39, L299.
- Sanchez, I. C. *Macromolecules* 1979, 12, 980.
- Post, C. B.; Zimm, B. H. *Biopolymers* 1979, 18, 1487; 1982, 21, 2123.
- Williams, C.; Brochard, F.; Frisch, H. L. *Annu. Rev. Phys. Chem.* 1981, 32, 433.
- Allegra, G.; Ganazzoli, F. *Macromolecules* 1983, 16, 1311; *J. Chem. Phys.* 1985, 83, 397.
- Slagowski, E.; Tsai, B.; McIntyre, D. *Macromolecules* 1976, 9, 687.
- Bauer, D. R.; Ullman, R. *Macromolecules* 1980, 13, 392.
- Swislow, G.; Sun, S. T.; Nishio, I.; Tanaka, T. *Phys. Rev. Lett.* 1980, 44, 796.
- Sun, S. T.; Nishio, I.; Swislow, G.; Tanaka, T. *J. Chem. Phys.* 1980, 73, 5971.
- Oyama, T.; Shiokawa, K.; Baba, K. *Polym. J.* 1981, 13, 167.
- Miyaki, Y.; Fujita, H. *Polym. J.* 1981, 13, 749.
- Stepanek, P.; Konak, C.; Sedlacek, B. *Macromolecules* 1982, 15, 1214.
- Post, C. B.; Zimm, B. H. *Biopolymers* 1982, 21, 2139.
- Perzynski, R.; Adam, M.; Delsanti, M. *J. Phys.* 1982, 43, 129.
- Perzynski, R.; Delsanti, M.; Adam, M. *J. Phys. (Paris)* 1984, 45, 1765.
- Vidakovic, P.; Rondelez, F. *Macromolecules* 1984, 17, 418.
- Park, I. H.; Wang, Q. W.; Chu, B. *Macromolecules* 1987, 20, 1965.
- Chu, B.; Park, I. H.; Wang, Q. W.; Wu, C. *Macromolecules* 1987, 20, 2833.
- Chu, B.; Xu, R. L.; Zuo, J. *Macromolecules* 1988, 21, 273.
- Park, I. H.; Fetters, L.; Chu, B. *Macromolecules* 1988, 21, 1178.
- (a) Chu, B.; Wang, Z. *Macromolecules* 1989, 22, 380. (b) Chu, B.; Wang, Z. *Macromolecules* 1988, 21, 2283.
- Kubota, K.; Fujishige, S.; Anod, I. *J. Phys. Chem.* 1990, 94, 5154.
- Mays, J. W.; Hadjichristidis, N.; Graessley, W. W.; Fetters, L. J. *J. Polym. Sci., Polym. Phys. Chem.* 1986, 24, 2553.
- Mays, J. W.; Hadjichristidis, N.; Fetters, L. J. *Macromolecules* 1985, 18, 2231.
- Selzer, J. C. *Macromolecules* 1985, 18, 585.
- Chiba, A.; Uzaka, S.; Uda, M.; Doi, S. *Rep. Prog. Polym. Phys. Jpn.* 1974, 17, 105.
- An extreme example of "noncollapse" is seen with the polychloroprene-methyl ethyl ketone system (Hanafusa, K.; Teramoto, A.; Fujita, A. *J. Phys. Chem.* 1966, 70, 4004) where solutions of high molecular weight polymer could be cooled to 45 °C below the  $\Theta$  temperature without phase separation.
- Cotts, P. M.; Selzer, J. C. *Macromolecules* 1990, 23, 2050.
- Morton, M.; Fetters, L. J. *Rubber Chem. Technol., Rubber Rev.* 1975, 48, 359.
- Riddick, J. A.; Bunger, W. B.; Sakano, T. K. *Organic Solvents: Physical Properties and Methods of Purification*; Wiley-Interscience: New York, 1986.
- Lindner, J. S. Ph.D. Dissertation, Mississippi State University, 1985.
- Lindner, J. S.; Wilson, W. W.; Mays, J. W. *Macromolecules* 1988, 21, 3304.
- Koppel, D. E. *J. Chem. Phys.* 1972, 54, 4814.
- Pusey, P. N. In *Photon Correlation and Light Beating Spectroscopy*; Cummins, H. Z., Pike, E. R., Eds.; Plenum: New York, 1973; p 387.
- Lindner, J. S.; Hadjichristidis, N.; Mays, J. W. *Polym. Commun.* 1989, 30, 174.
- Batchelor, G. K. *J. Fluid Mech.* 1977, 83, 97.
- Flory, P. J. *Principles of Polymer Chemistry*; Cornell University: Ithaca, NY, 1953.
- Noda, I.; Mizutani, K.; Kato, T.; Fujimoto, T.; Nagasana, M. *Macromolecules* 1970, 3, 787.
- Cowie, J. M. G.; Bywater, S. *J. Polym. Sci.* 1970, C30, 85.
- Noda, I.; Mizutani, K.; Kato, T. *Macromolecules* 1977, 10, 618.
- Douglas, J. F.; Roovers, J.; Freed, K. F. *Macromolecules* 1990, 23, 4168.
- Oono, J. *J. Chem. Phys.* 1983, 79, 4629.
- Pyun, C. W.; Fixman, M. *J. Chem. Phys.* 1965, 42, 3838.
- Cherayil, B. J.; Douglas, J. F.; Freed, K. F. *J. Chem. Phys.* 1985, 83, 5293.

**Registry No.** P $\alpha$ MS, 25014-31-7; cyclohexane, 110-82-7.